



# **Numerical Simulation of the Friction Stir Welding Process using Lagrangian, Eulerian & ALE Approaches**

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# Overview

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- Background
  - The Friction Stir Welding Process
  - Modeling of FSW
- Numerical models : FORGE3<sup>®</sup> & THERCAST<sup>®</sup>
- Modeling and experimental results
  - Plunging phase : comparison between experimental and numerical result
  - Welding phase :  
Lagrangian / Eulerian simulations capabilities
  - ALE formulation and first results
- Future work

A 3D wireframe scene featuring a central orange cylinder and a larger, semi-transparent structure in the background. The scene is rendered with a green-to-cyan color gradient and a dense network of gray lines forming a mesh. The word "Background" is written in bold black text across the center of the image.

**Background**

# The Process

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### 1. Plunging phase

Plunge experiment  
FORGE3® simulation  
Comparison

### 2. Welding phase

Eulerian Simulation  
Lagrangian Simulation

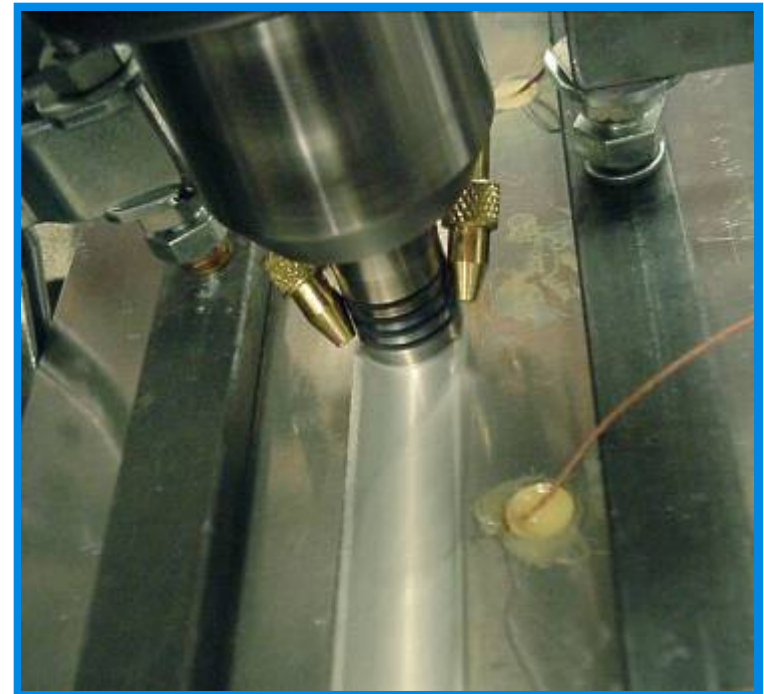
### 3. ALE formulation

Different descriptions  
The two main steps  
Dwelling phase

Future Work

## ➤ Friction Stir Welding Process

- Patented in 1991 by TWI
- A solid-state joining process
- Potential commercial and military users
  - aerospace
  - automotive
  - marine
- Capable of joining aluminum, steel, stainless steel



- Different main phases of FSWP

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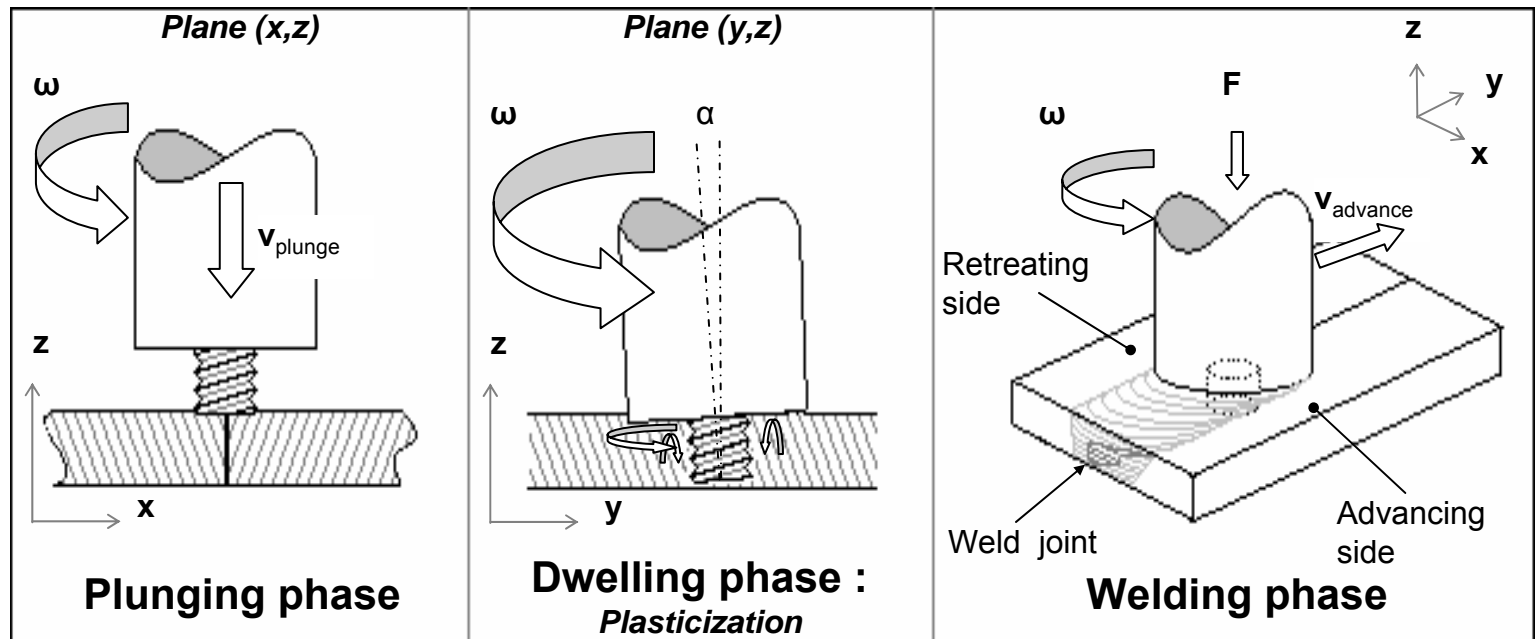
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# Modeling of FSW

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## ➤ Motivation:

- Predict material flow: try to minimize heat input, and eliminate defects
- Use to develop better tooling designs
- Predict mechanical properties of weld:  
flow & thermal history  
=> mechanical properties and eventually  
microstructure



# Approaches in literature

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- CFD approach: obtain information on material flow, but neglect free surface deformation and effect of deformation history
- Lagrangian FE:
  - use analytical heat source and apply a compressive stress along the weld line; calculate residual stresses
  - simulate material flow, including heat from friction and material deformation; requires complex remeshing
- Arbitrary Lagrangian Eulerian (ALE) FE: can simulate flow and include heat from friction and deformation; avoids degeneration of mesh; allows for deformation of free surface

A 3D visualization of a numerical model, likely a finite element analysis (FEA) mesh. The model consists of a large cylindrical structure with a smaller cylindrical hole in the center. The mesh is composed of numerous small, interconnected triangular elements. The color of the mesh transitions from a light green at the top to a dark red at the bottom, indicating a stress or temperature gradient. The text "Numerical Models" is overlaid in the center of the image.

# Numerical Models



# FORGE3<sup>®</sup> & THERCAST<sup>®</sup>

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Future Work

- Hot, warm, and cold forging (FORGE3<sup>®</sup>)  
Filling and cooling of foundry parts (THERCAST<sup>®</sup>)
- 3D thermo-mécanical computation
- **Lagrangian** (FORGE3<sup>®</sup>) and /or **ALE** (THERCAST<sup>®</sup>) Finite Element Formulation
- Automatic Remeshing

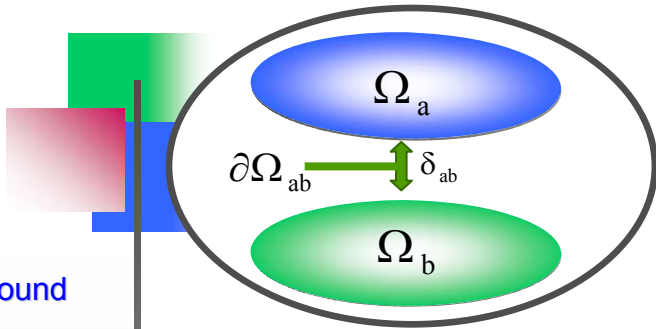
## • Strong form of the mechanical problem :

Pure viscoplastic behaviour (firstly) with thermal coupling

$$\begin{cases} \dot{\boldsymbol{\varepsilon}} = \dot{\boldsymbol{\varepsilon}}_{vp} + \dot{\boldsymbol{\varepsilon}}_{th} \\ \mathbf{s} = \boldsymbol{\sigma} + p\mathbf{I} = 2K_{(T,\bar{\varepsilon})} \left( \sqrt{3} \dot{\boldsymbol{\varepsilon}} \right)^{m_{(T,\bar{\varepsilon})}-1} \dot{\boldsymbol{\varepsilon}}_{vp} \\ \dot{\boldsymbol{\varepsilon}}_{th} = \alpha \dot{T} \mathbf{I} \end{cases}$$

Incompressibility and equilibrium  $\Rightarrow$  
$$\begin{cases} \text{tr}(\dot{\boldsymbol{\varepsilon}}_{vp}) = \text{div } \mathbf{v} - 3\alpha \dot{T} = 0 \\ \nabla \cdot \boldsymbol{\sigma} + \rho \mathbf{g} - \rho \boldsymbol{\gamma} = \nabla \cdot \mathbf{s} - \nabla p + \rho \mathbf{g} - \rho \boldsymbol{\gamma} = 0 \end{cases} \quad + \text{B.C.}$$

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Contact equation :

$$\begin{cases} 0 \leq \delta_{ab}^{t+\Delta t} \\ \delta_{ab}^{t+\Delta t} \approx \delta_{ab}^t - (\mathbf{v}_a^t - \mathbf{v}_b^t) \cdot \mathbf{n}_{ab}^t \Delta t \end{cases}$$

$$\Rightarrow (\mathbf{v}_a^t - \mathbf{v}_b^t) \cdot \mathbf{n}_{ab}^t - \frac{\delta_{ab}^t}{\Delta t} \leq 0$$

Norton friction equation :

$$\begin{cases} \text{si } \sigma_n < 0 \text{ alors } \boldsymbol{\tau} = -\alpha_f K_{(\bar{\epsilon}, T)} \|\Delta \mathbf{v}_g\|^{p_f - 1} \Delta \mathbf{v}_g \\ \text{avec } \Delta \mathbf{v}_g = (\mathbf{v}_a - \mathbf{v}_b) - ((\mathbf{v}_a - \mathbf{v}_b) \cdot \mathbf{n}_{ab}) \mathbf{n}_{ab} \end{cases}$$

• Strong form of the thermal problem :

Heat Equation

$$\rho c \frac{dT}{dt} - \text{div}(k \nabla T) = \dot{W} \quad \text{dans } \Omega \quad ; \quad \text{avec } \dot{W} = \boldsymbol{\sigma} : \boldsymbol{\epsilon} \quad + \text{B.C.}$$

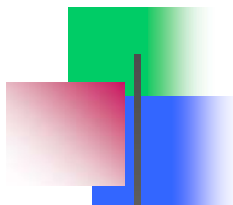
» Heat transfert by convection/radiation :

$$-k \nabla T \cdot \mathbf{n} = h_{cr} (T + T_{ext})$$

» Conduction with tools and heat due to friction :

$$-k \nabla T \cdot \mathbf{n} = -h_{cd} (T + T_{tool}) + \frac{b}{b + b_{tool}} \boldsymbol{\tau} \cdot \mathbf{v}_g$$

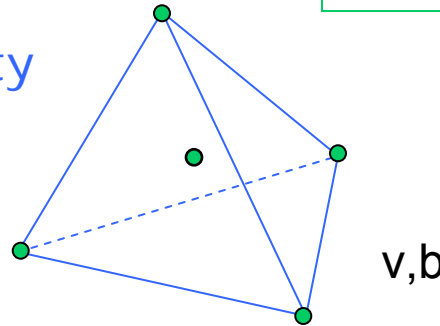
Heat Sources



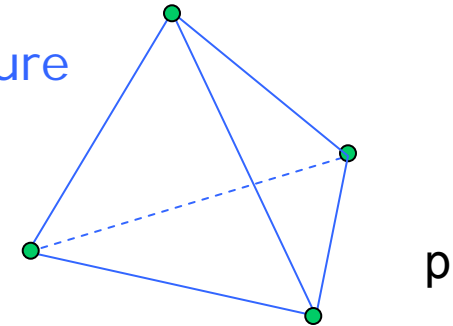
- Finite Element discretisation & FORGE3<sup>®</sup> solveur

P1+/P1

Velocity



Pressure



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- Time discretisation

$$X^{t+\Delta t} = X^t + V^t \Delta t$$

- Newton-Raphson algorithm

→  $R^t(V^t, P^t) = 0$

- Preconditioned Conjugate Gradient solver
- Parallel resolution by mesh partitioning
- Updated Lagrangian formulation  
with automatic remeshing (topological, MTC)



# **Modeling and experimental results**

# Plunging phase

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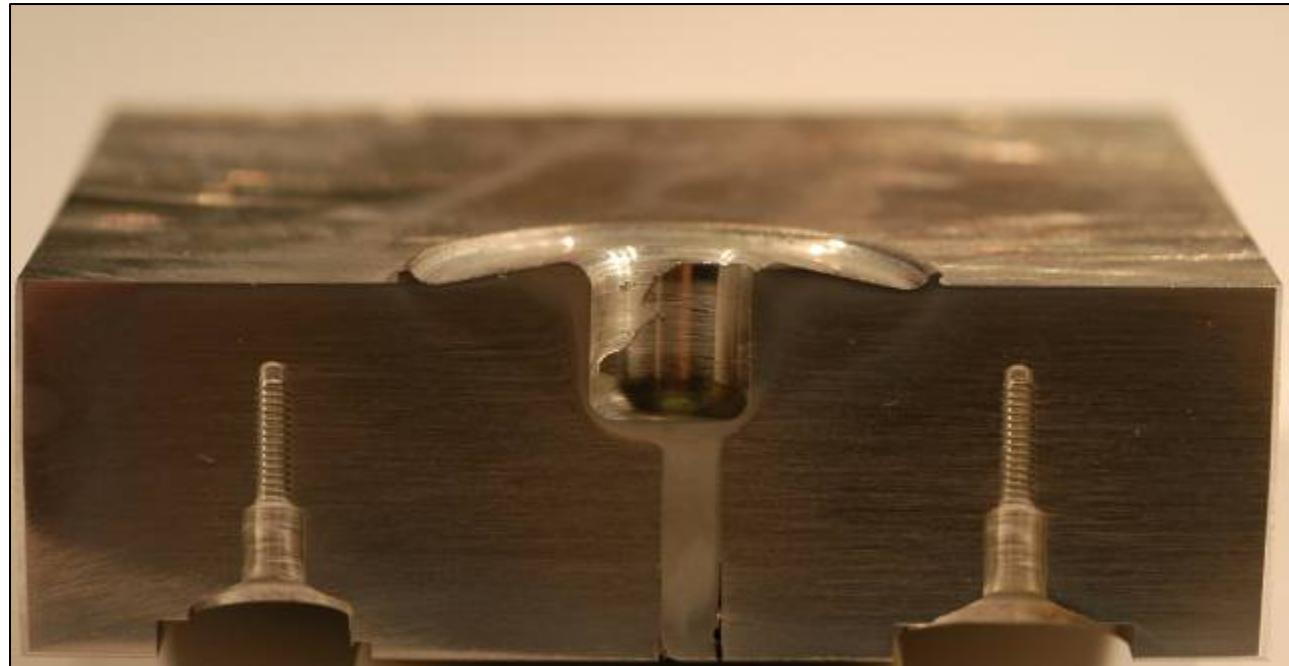
#### Dwelling phase

## Future Work

## ➤ Plunge experiment

- Thermocouples

- Weld Material—12.7 mm to 20.6 mm radius, at a depth of 1.6 mm
- FSW Tool—1.2 mm of depth



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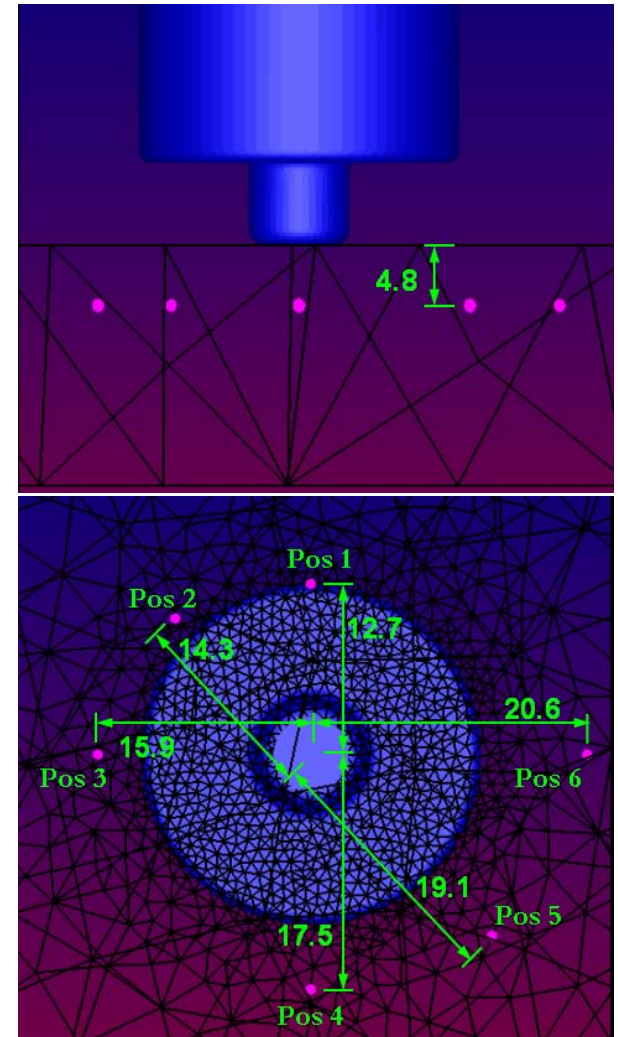
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## ➤ FORGE3® simulation

- 6 Second Plunge  
1.19 mm/s plunge speed, 600 RPM
- Lagrangian sensors were placed in the FSW weld material (1.6 mm)
- Remesh every 4 time steps
- Adiabatic contact heat transfer condition, Convective cooling on free surfaces



# ➤ Comparison : experimental / numerical results

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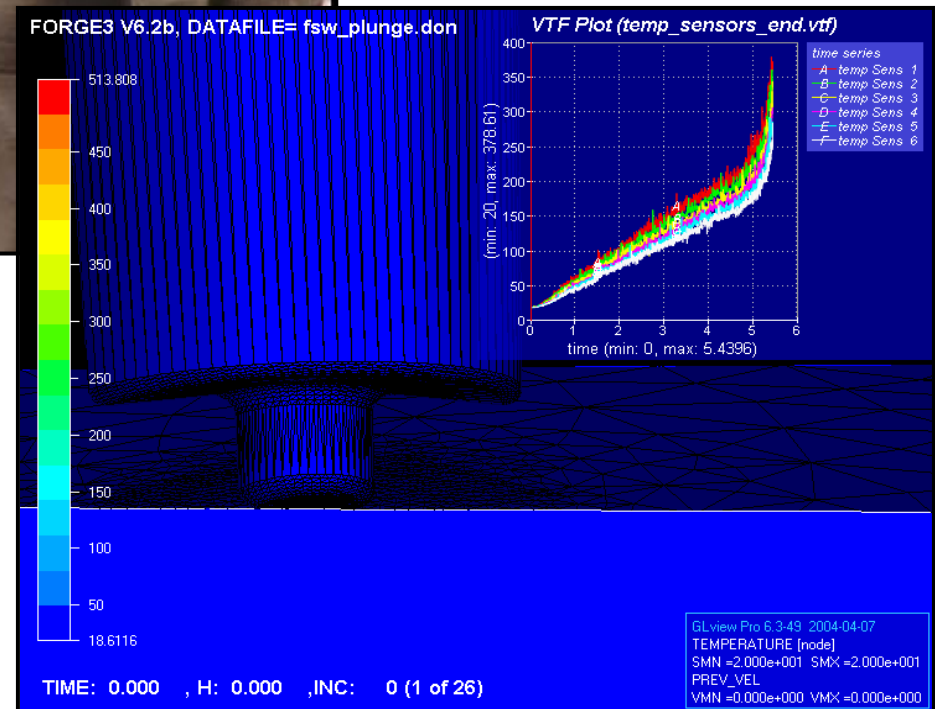
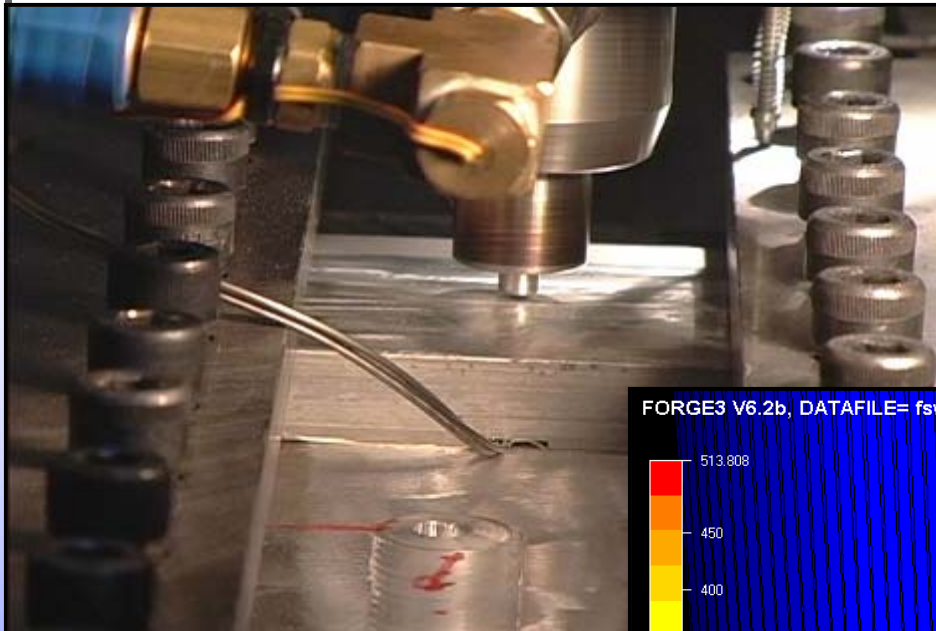
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# • Workpiece Temperature Rise

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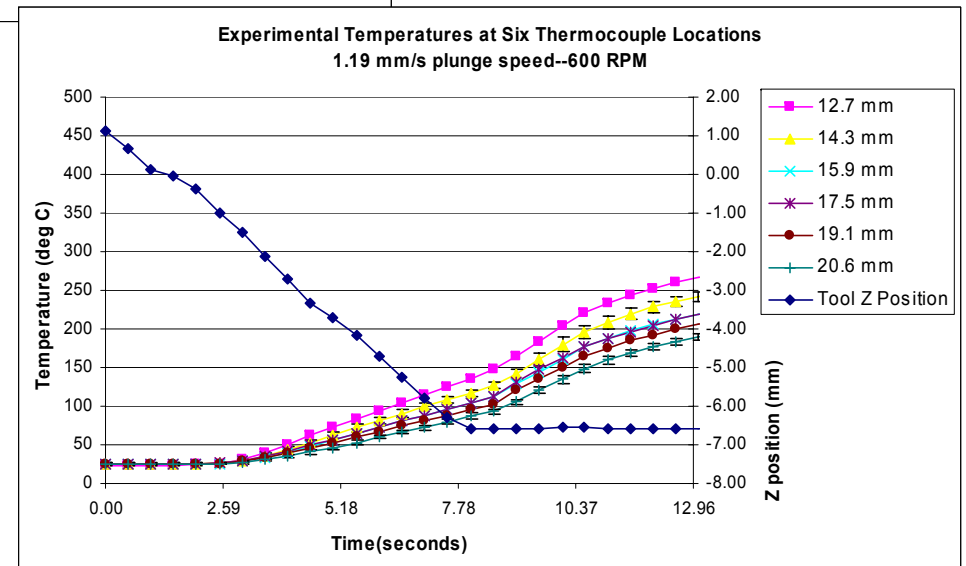
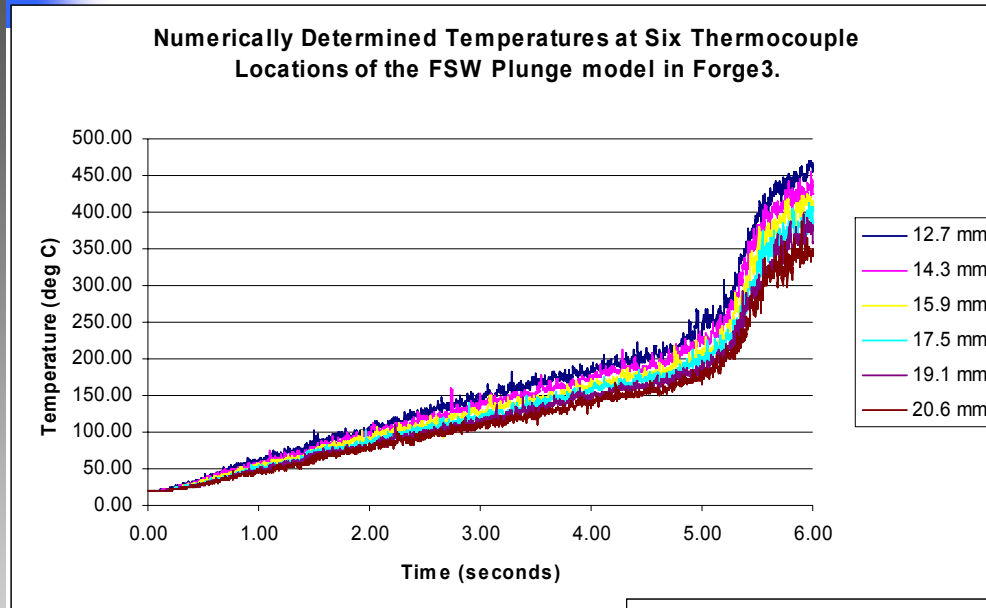
### 2. Welding phase

- Eulerian Simulation
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Future Work





- Workpiece Temperature Rise

- Weld Material Temperature Profiles

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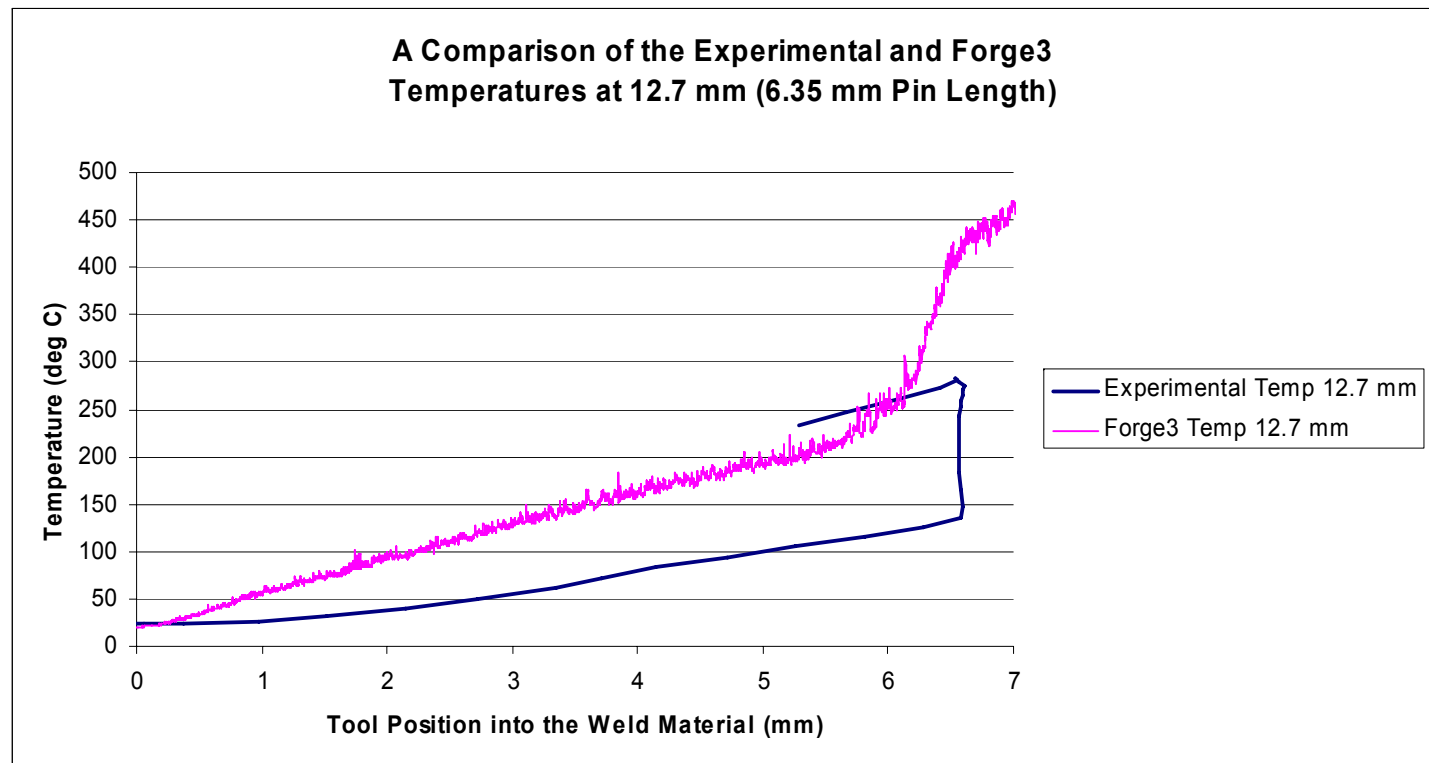
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# • Tool Temperature and Workpiece Isotherms

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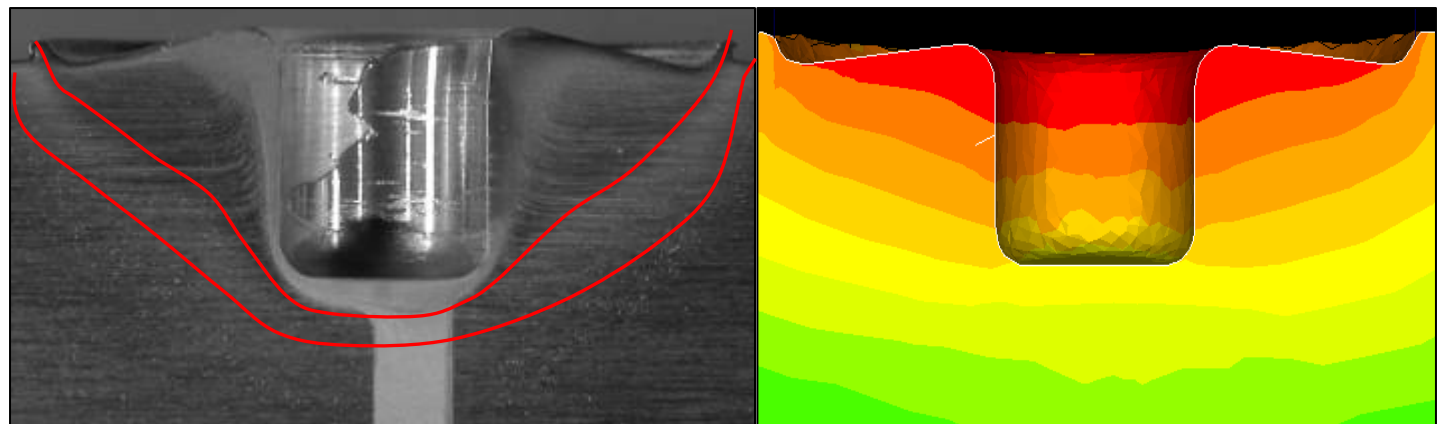
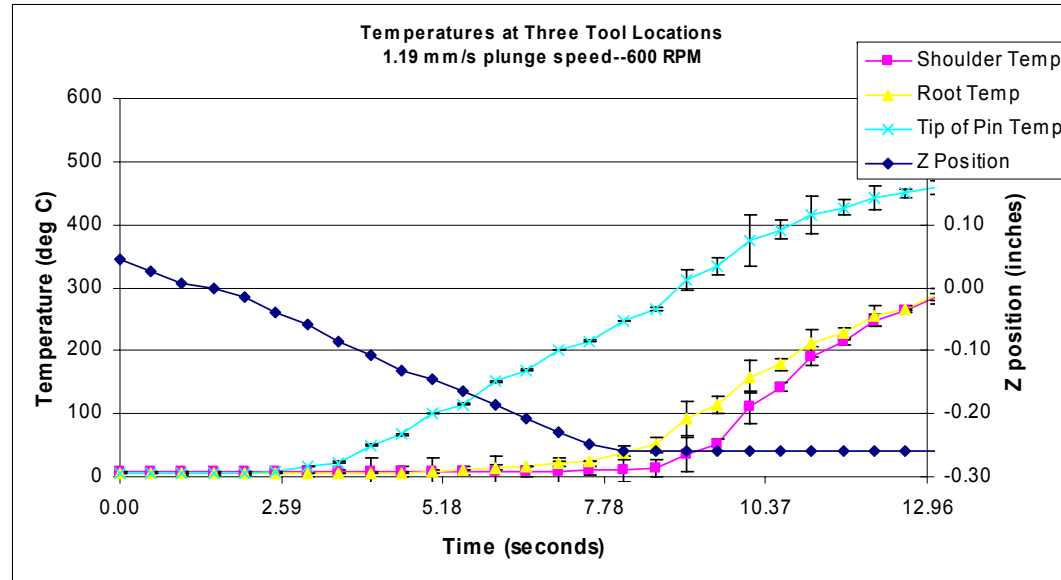
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# Welding phase

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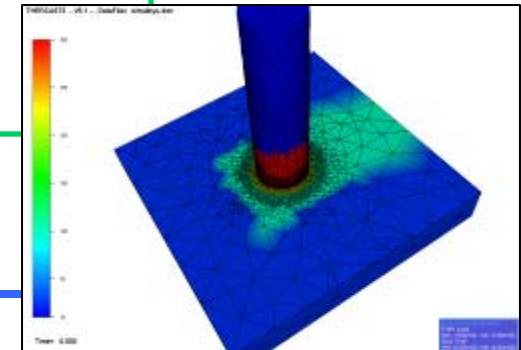
### 3. ALE formulation

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## Geometric data :

- part : 127mm x 127mm x 19mm
- experimental welding tool (concave shoulder, 3° tilted) :
  - pin :  $\varnothing=8\text{mm}$  ,  $h=7\text{mm}$
  - shoulder :  $\varnothing=25.4\text{mm}$ ,  $h=90\text{mm}$   
(cooling  $\rightarrow 10^\circ\text{C}$  forced on 60mm from the top surface)
  - rotational speed : 15 rotation/second
  - advance speed : 5 mm/second



## Thermal and mechanical data :

- Convective exchange with air on all surfaces ( $h_{cr}=30 \text{ W/m}^2$ )
- Same standard behavior law for aluminum
- Norton viscoplastic law : coefficient  $\alpha_f$  from 0.6 at  $0^\circ\text{C}$  to 1.1 at  $650^\circ\text{C}$  (linear evolution)  
q from 1 at  $0^\circ\text{C}$  to 0.5 at  $650^\circ\text{C}$  (linear evolution)
- Density, conductivity, and heat capacity in paper

# ➤ Pure Eulerian Simulation : neglect of free surfaces movement / no remeshing

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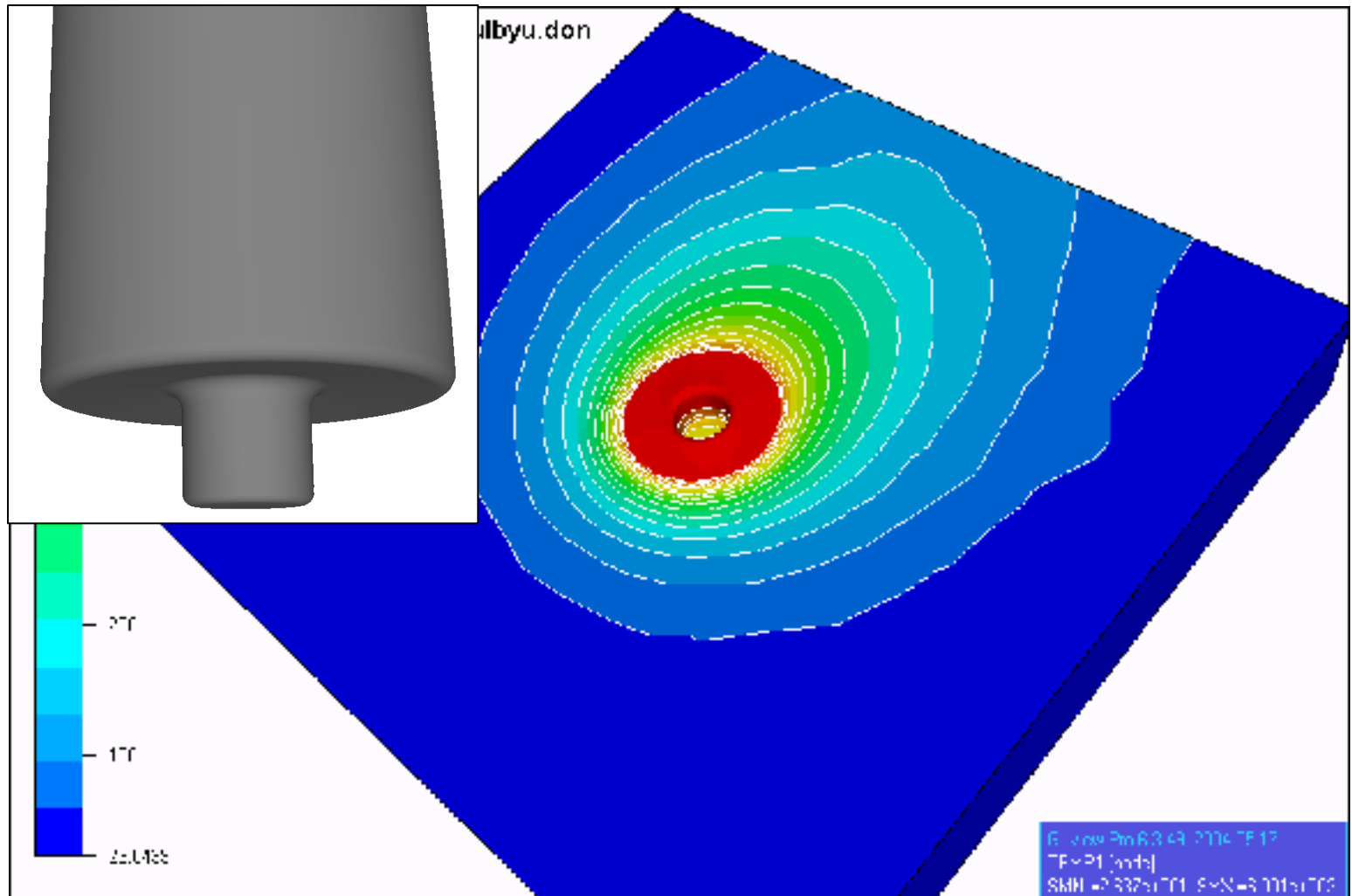
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6s simulation with an arbitrary initial temperature

- 6s simulation with an arbitrary initial temperature field

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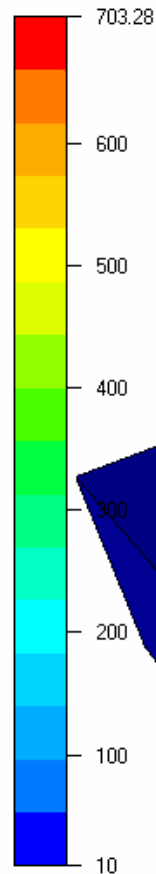
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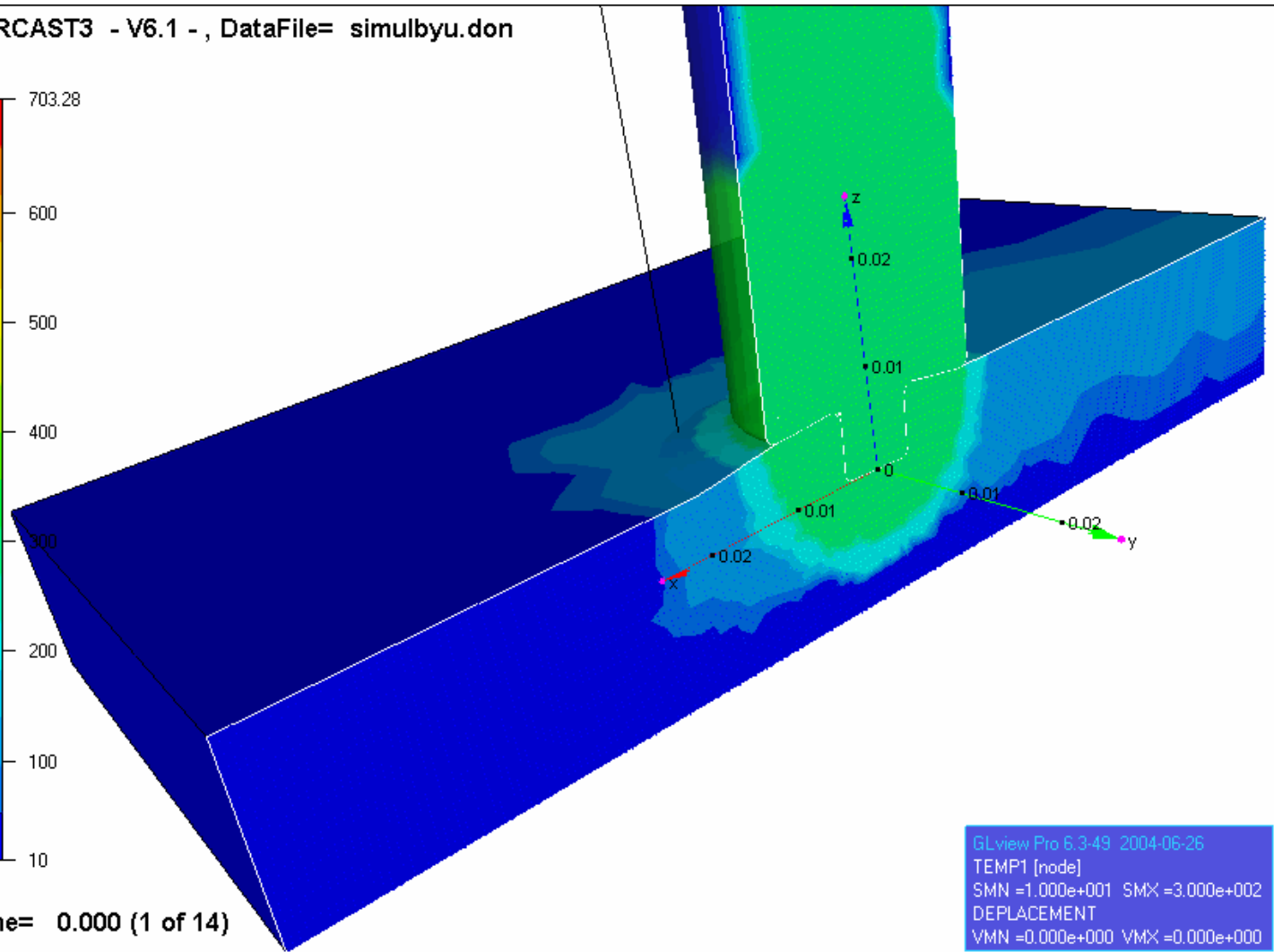
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Future Work

THERCAST3 - V6.1 - , DataFile= simulbyu.don



Time= 0.000 (1 of 14)



GLview Pro 6.3-49 2004-06-26  
TEMP1 [node]  
SMN =1.000e+001 SMX =3.000e+002  
DEPLACEMENT  
VMN =0.000e+000 VMX =0.000e+000

avance eul exp

# ➤ Lagrangian capabilities : simulation of a defect during “cold welding”

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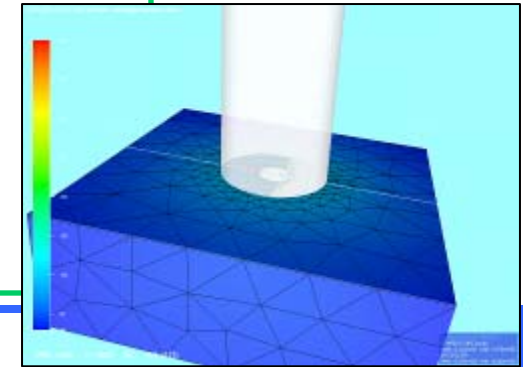
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### Geometric data :

- part : 60mm x 60mm x 20mm
- simplified welding tool (no concave shoulder, 3° tilted) :
  - pin :  $\varnothing=6\text{mm}$  , h= 6mm
  - shoulder :  $\varnothing=20\text{mm}$ , h=60mm
  - rotational speed : 15 rotation/second
  - advance speed : 1 mm/second



### Thermal and mechanical data :

- Adiabatic rigid tool ➔ heat due to friction and plastic deformation only
- Standard behavior law for aluminum in hot forming process (Hansel Spittel law) :

$$\sigma_f = A e^{-0.0479T} \bar{\varepsilon}^{-0.01383} \dot{\bar{\varepsilon}}^{0.09964} e^{\frac{-0.0011}{\bar{\varepsilon}}}$$

- “Strong” friction (Coulomb law) :

$$\begin{cases} \tau = 0.3 \sigma_n \frac{\Delta v}{\|\Delta v\|} & \text{if } 0.3 \sigma_n < K_{(T,\varepsilon)} \\ \tau = 0.6 K_{(T,\varepsilon)} \frac{\Delta v}{\|\Delta v\|} & \text{if } 0.3 \sigma_n > 0.6 K_{(T,\varepsilon)} \end{cases}$$

- 6s simulation with a low low initial temperature

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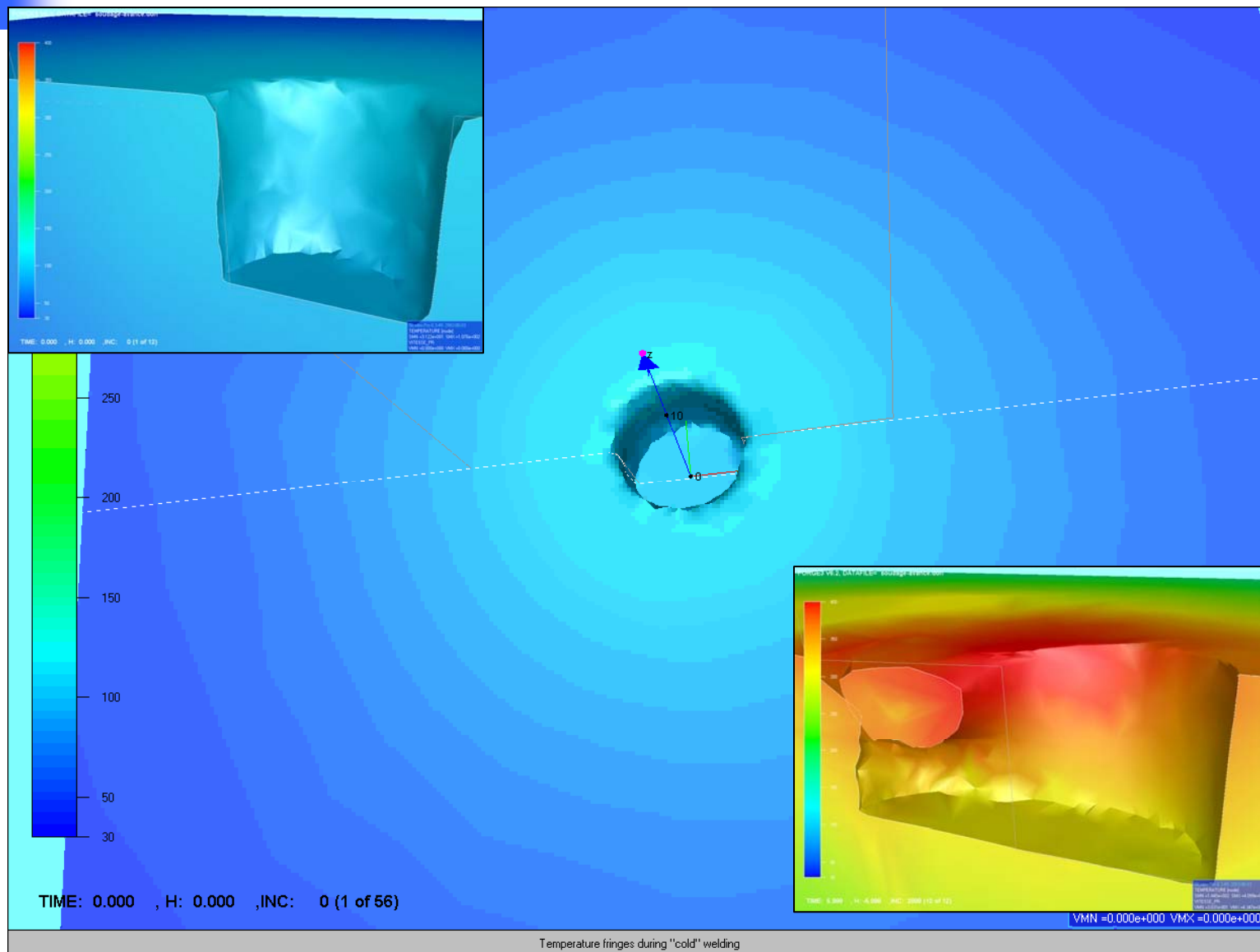
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# ALE formulation

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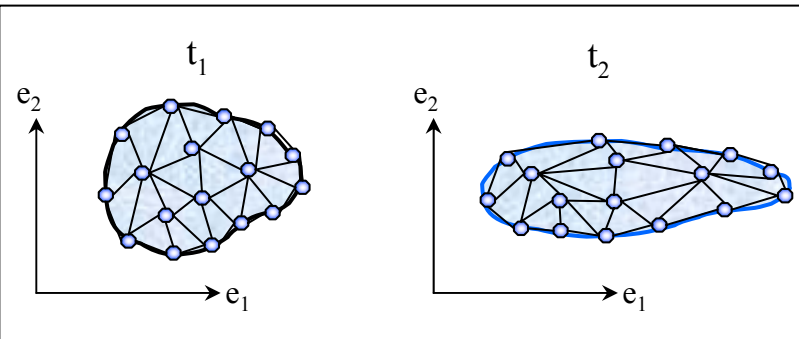
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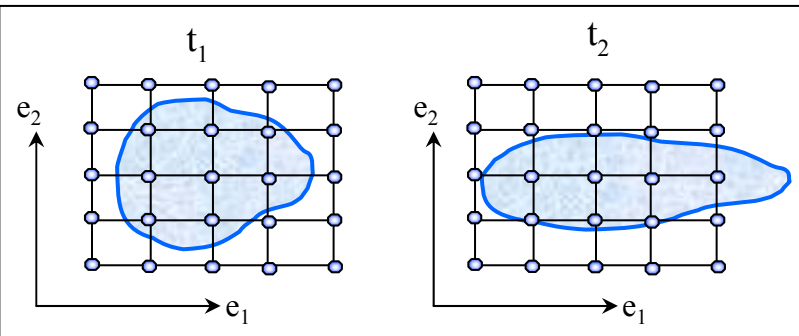
Future Work

## ➤ Different Descriptions :

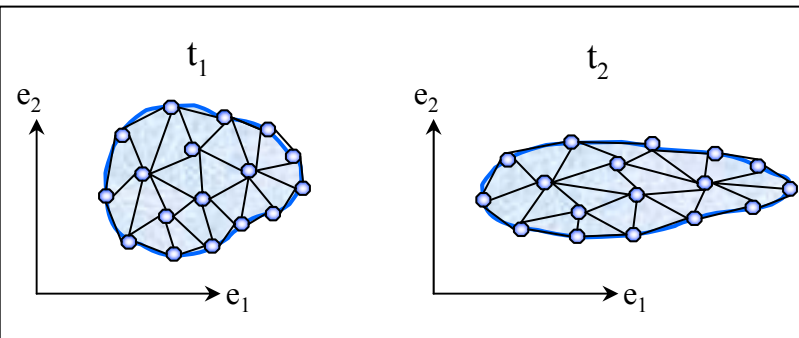
Lagrangian mesh



Eulerian mesh



ALE mesh





# The two main steps of the ALE description implemented in Theracast :

- Convective terms treatment

$$\begin{cases} \frac{d\varphi}{dt} = \frac{d_g \varphi}{dt} + \mathbf{c} \cdot \nabla \varphi \\ \mathbf{c} = \mathbf{v} - \mathbf{w} \end{cases}$$

$\mathbf{v}$  : material velocity  
 $\mathbf{w}$  : mesh velocity

Splitting Method ( used firstly )

= lagrangian iteration + transport on the new mesh

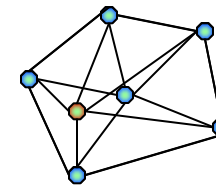
Convective Approach (upwind aspect )

$$\varphi_{ALE}^{t+\Delta t} = \varphi_{ref}^t + \int_{\Delta t} \frac{d_g \varphi}{dt}$$

No Updated Lagrangian Mesh construction

→ Mesh velocity computation : w

Velocity Centering Method



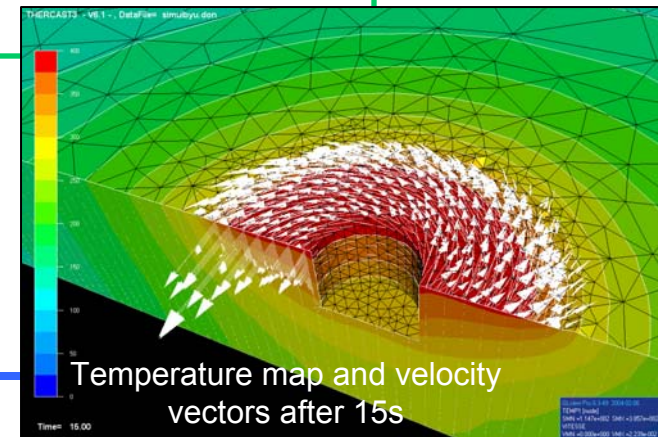
ALE

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# ➤ ALE simulation of the dwelling phase

## Geometric data :

- part : 127mm x 127mm x 19mm
- simplified tool (no concave shoulder, not tilted) :
  - pin :  $\varnothing=8\text{mm}$  ,  $h=7\text{mm}$
  - shoulder :  $\varnothing=25.4\text{mm}$ ,  $h=90\text{mm}$   
(cooling  $\rightarrow 10^\circ\text{C}$  forced on 60mm from the top surface)
  - rotational speed : 15 rotation/second
  - no advance speed



## Thermal and mechanical data :

- Exchange with bottom plate model by a coefficient  $h_{cr}=300 \text{ W/m}^2$  and exchange with air on other surfaces ( $h_{cr}=30 \text{ W/m}^2$ )
- Same standard behavior law for aluminum
- Norton viscoplastic law
- Density, conductivity, and heat capacity depend on temperature

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- 15s simulation without any remeshing  
 → stability of ALE formulation  
 (Initial temperature obtained after plunging phase)

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### 2. Modeling of FSW

## II. Numerical models FORGE3® & THERCAST®

## III. Modeling and experimental results

### 1. Plunging phase

Plunge experiment  
 FORGE3® simulation  
 Comparison

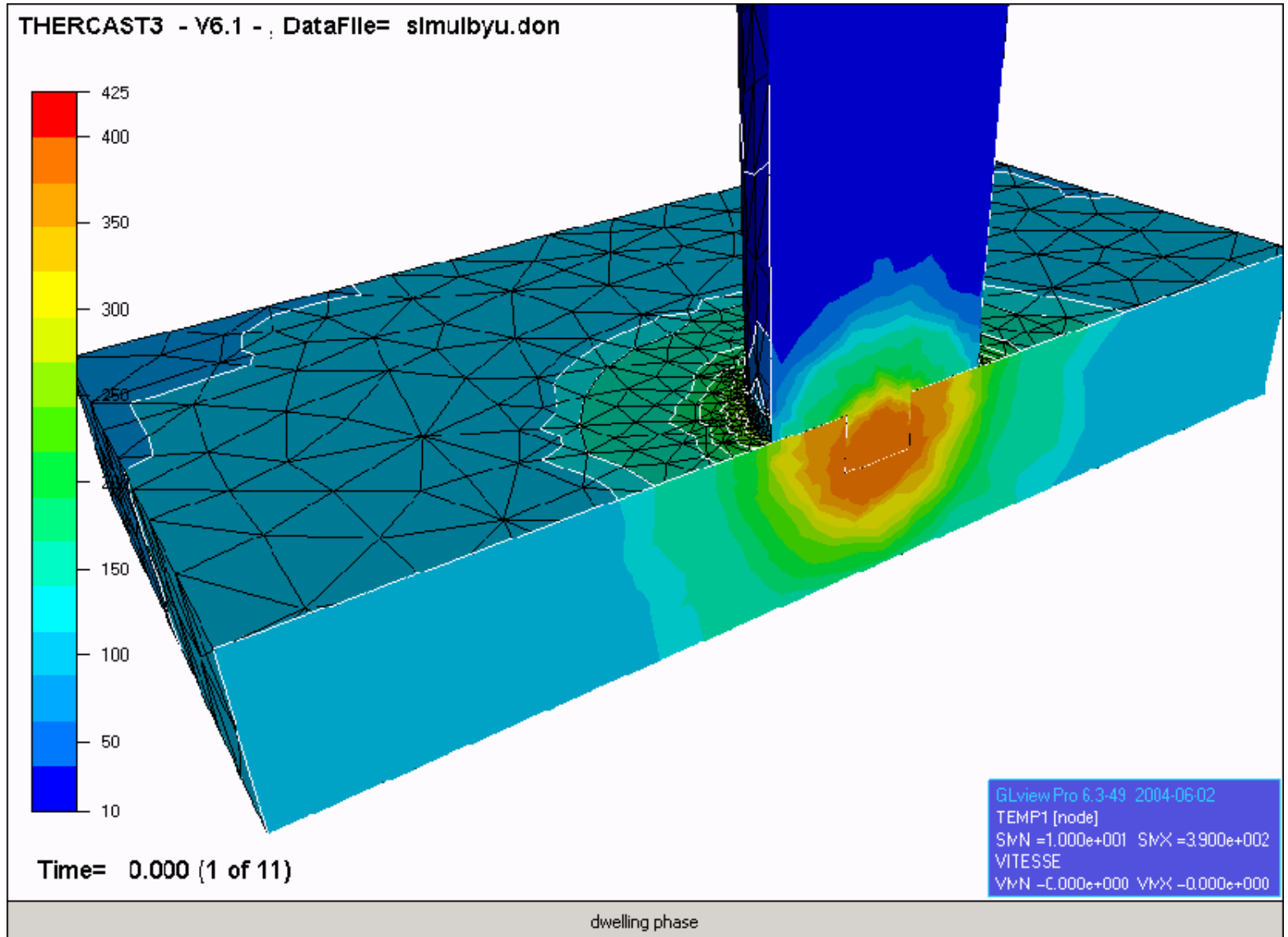
### 2. Welding phase

Eulerian Simulation  
 Lagrangian Simulation

### 3. ALE formulation

Different descriptions  
 The two main steps  
 Dwelling phase

## Future Work



# • Comparison with experimental results

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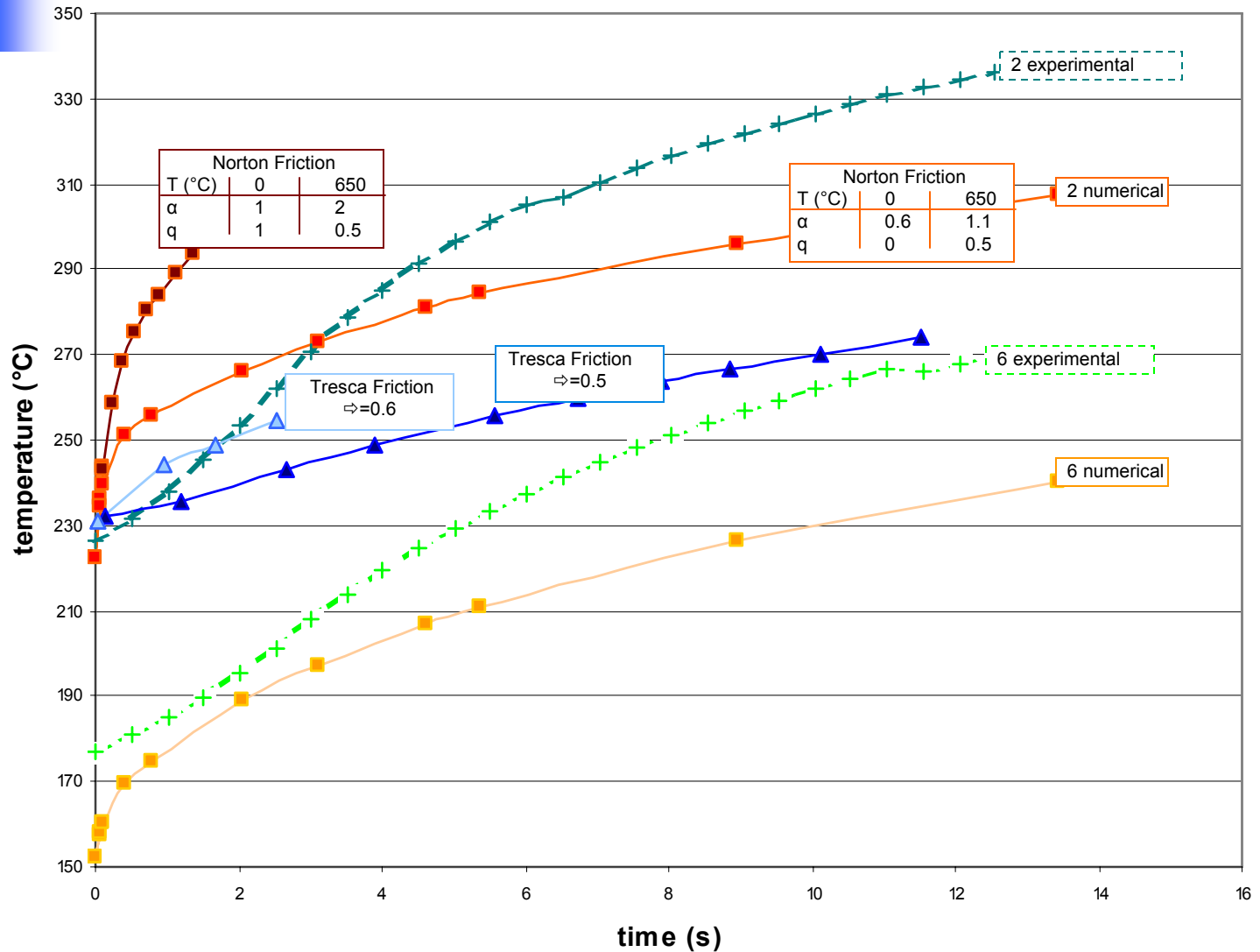
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# Summary

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## Future Work

- Lagrangian, Eulerian, and ALE approaches have been used to simulate FSW, using Forge3® and Thericast®
- The ALE approach is best adapted for modeling this process, because it takes into account changes in the free surface while avoiding element degeneration in high deformation zones

## Future Work

- Implementation of a complete ALE formulation in Forge3® code
- Test of different transport techniques :
  - nodal upwind
  - SUPG
  - MLS / RBFwith use of adaptive remeshing to minimize transport diffusion
- Further comparison between experiment and simulation
- Experimental work to study friction, material behavior, and heat transfer coefficients